

normalization factors for generalized gaussians:

$$\int_{-\infty}^{\infty} e^{-\frac{x^2}{a}} dx = \sqrt{\pi a}$$

$$\int_{-\infty}^{\infty} e^{-\frac{x^2}{a} - ikx} dx = e^{-\frac{k^2 a}{4}} \sqrt{\pi a}$$

gaussian evolution:

$$\psi = e^{-\frac{(x-x_c)^2}{a} - ik(x-x_c) + c} = g e^{-\frac{(x-x_c)^2}{a} - ik(x-x_c)}; \quad g = e^c$$

$$\mathcal{H} = -\frac{1}{2m} \frac{\partial^2}{\partial x^2} + v_0 + v_1(x - x_c)$$

$$i\psi \left( \frac{\dot{a}}{a^2} (x - x_c)^2 + 2(x - x_c) \frac{\dot{x}_c}{a} - i\dot{k}(x - x_c) - ik\dot{x}_c + \dot{c} \right) = \\ (v_0 + v_1(x - x_c) - \frac{2}{a^2 m} (x - x_c)^2 - \frac{k^2}{2m} + \frac{2ik}{ma} (x - x_c) + \frac{1}{ma}) \psi$$

$$\begin{cases} a' &= -\frac{2i}{m} \\ x'_c &= \frac{k}{m} \\ k' &= -v_1 \\ c' &= iv_0 - \frac{ik^2}{2m} + \frac{i}{ma}; \end{cases} \quad g' = c'g$$

sampling for gaussian functions

$$\int_{-\infty}^{\infty} e^{-\frac{(y-z)^2}{p} -iky} e^{-\frac{z^2}{q}} dz = \int_{-\infty}^{\infty} e^{-\frac{p+q}{pq}\theta^2 - \frac{y^2}{p+q} -iky} d\theta = \sqrt{\pi \frac{pq}{p+q}} e^{-\frac{y^2}{p+q} -iky}; \quad \theta = z - \frac{q}{p+q}y$$

$$\int_{-\infty}^{\infty} e^{-\frac{(y-z)^2}{p} -iky} e^{-\frac{z^2}{q}} dz = g e^{-\frac{(x-x_c)^2}{a} - ik(x-x_c)}$$

$$\begin{cases} a &= p + q \\ g &= \sqrt{\pi \frac{pq}{p+q}} \\ y &= x - x_c \end{cases}$$